

M.Sc. (Previous) DEGREE EXAMINATION, DECEMBER 2008.

First Year

Physics

Paper I — MATHEMATICAL PHYSICS

Time : Three hours

Maximum : 100 marks

Answer any FIVE of the following. (5 × 20 = 100)

1. (a) Starting from the Legendre's differential equation prove the orthogonal property. (12)
 (b) Find the values of Bessel function $J_{+3/2}(x)$ and $J_{-3/2}(x)$. (8)

2. (a) Starting from generating function of Hermite polynomials prove that

$$H_{n-1}(x) = 2xH_n(x) - 2nH_{n-1}(x). \quad (10)$$
 (b) Using Leguerre polynomials prove

$$(n+1)L_{n+1}(x) - (2n+1-x)L_n(x) - nL_{n-1}(x) = 0. \quad (10)$$

3. (a) State and prove Laurent theorem. (12)
 (b) Expand $f(z) = \sin z$ in a Taylor series about $z = \pi/4$. (8)

4. (a) State and prove Cauchy-Riemann equations. (12)
 (b) Prove that $u = e^{-x}(x \sin y - y \cos y)$ is harmonic. (8)

5. (a) Define outer product, inner product and contraction of tensors with given examples. (10)
 (b) Show that if A_{rs}^{pq} is a tensor, then $A_{rs}^{pq} + A_{sr}^{qp}$ is a symmetric tensor and $A_{rs}^{pq} - A_{sr}^{qp}$ is a skew symmetric tensor. (10)

6. (a) Obtain the expression for three dimensional elasticity of a crystal using tensors. (12)
 (b) Show that the Kronocker delta function is a mixed tensor of rank two. (8)

7. (a) Solve the equation $\frac{dx^2}{dt^2} - 2\frac{dx}{dt} + x = c^t$ with $x = 2$ and $\frac{dx}{dt} = -1$ and $t = 0$ using Laplace transformation. (10)
 (b) Find the Laplace transform of $\sin^3 2t$ and $t^3 e^{-3t}$. (10)

8. (a) Find the Fourier sine and cosine transform of $2e^{-5x} + 5e^{-2x}$. (12)
 (b) Obtain the Fourier transform of Dirac delta function. (8)

9. Answer any TWO of the following : (2 × 10 = 20)
 (a) State and prove Cauchy's integral formula
 (b) Prove that $\pi J_n(x) = \int_0^{\frac{\pi}{2}} \cos(n\theta - x \sin \theta) d\theta$ using Bessel function.
 (c) Show that

$$(l + 1) P_{l+1}(x) - (2l + 1) x P_l(x) + l P_{l-1}(x) = 0.$$

- (d) Mention the different types of tensors. Give the transformation laws for tensor of 3rd rank.

wk 7

(DPHY 02)

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Paper II — CLASSICAL MECHANICS AND STATISTICAL MECHANICS

Time : Three hours

Maximum : 100 marks

Answer any FIVE questions.

All questions carry equal marks.

1. (a) Distinguish between conservative and non-conservative mechanical systems. Obtain Lagrange's equations of motion for a conservative system using D'Alembert's principle.
(b) Explain the principle of least action.
2. (a) What are Eulerian angles? Explain their importance.
(b) Obtain the relation between the angular momentum and kinetic energy of a rigid body.
3. (a) Derive the Hamilton-Jacobi partial differential equation and discuss the physical significance of the Hamilton's generating function.
(b) Explain the importance of action angle variables.
4. (a) Formulate the theory of small oscillations.
(b) Determine the normal modes and frequencies of vibrations of a linear triatomic molecule.
5. (a) What is a micro-canonical ensemble? Obtain the equipartition theorem.
(b) Explain Gibb's paradox.
6. (a) Explain energy fluctuations in a Canonical ensemble.
(b) Discuss the equivalence between the canonical ensemble and grand canonical ensemble.
7. (a) Give a brief account of the postulates of quantum statistical mechanics.
(b) Explain the third law of thermodynamics.
8. (a) Obtain the equation of state of an ideal Fermi gas.
(b) Explain the salient features of Bose-Einstein condensation.
9. Write notes on any TWO of the following :
 - (a) Cyclic coordinates.

- (b) Lorentz transformation.
 - (c) Density fluctuations in grand canonical ensemble.
 - (d) Partition function.
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(DPHY 03)

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Paper III — QUANTUM MECHANICS

Time : Three hours

Maximum : 100 marks

Answer any FIVE questions.

All questions carry equal marks.

1. (a) Define the terms 'eigen function' 'expectation value' and 'degenerate eigen functions' with examples.
(b) State and prove Ehrenfest theorem.
2. (a) Discuss the motion of an electron across a potential step of finite height. Calculate the reflection and transmission coefficients.
(b) Obtain the eigen functions and eigen values for a rigid rotator.
3. (a) Obtain first and second order wave functions for time independent perturbation theory.
(b) Apply perturbation theory to explain Stark effect in hydrogen atom.
4. (a) What is variation principle? Apply this principle to explain the ground state of helium atom.
(b) Explain sudden and adiabatic approximations.
5. (a) Prove that the operators \hat{L}^2 and \hat{L}_z commute but \hat{L}_x and \hat{L}_y do not commute. Discuss the physical significance of these commutation relations.
(b) Explain spin angular momentum and obtain Pauli spin matrices.
6. (a) What are Clebsch - Gordon coefficients? Explain their properties.
(b) State and prove Wigner - Eckart theorem.
7. (a) Obtain the equation of motion for an operator in Heisenberg picture and bring out the condition for a dynamical variable to be a constant of motion.
(b) Obtain Dirac's relativistic equation for a particle.

8. Write short notes on any TWO of the following :

- (a) Bra and ket notation.
- (b) WKB method.
- (c) Matrices for J^2 and J_x
- (d) Klein Gordon equation.

(DPHY 04)

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Paper IV — ELECTRONICS

Time : Three hours

Maximum : 100 marks

Answer any FIVE questions.

All questions carry equal marks.

1. (a) With a neat diagram, explain the working of a difference amplifier.
(b) Discuss the operation of a voltage follower.
2. (a) Draw the circuit of 555 timer and explain how different types of waves can be generated.
(b) Explain the working of class B push pull amplifier.
3. (a) Discuss TEM wave propagation in coaxial line resonant cavities.
(b) What is magic T? Explain its features.
4. (a) Draw the block diagram of superheterodyne receiver and explain its working.
(b) Give a brief account of sky wave propagation.
5. (a) Draw the circuits of NAND, NOR and EX-OR gates and draw their truth tables.
(b) Explain the working of multiplexer encoder with a neat circuit.
6. (a) Discuss the working of synchronous and asynchronous counters with neat sketches.
(b) Explain the working of D/A converters with a neat circuit.
7. (a) With suitable examples explain the addressing modes of 8085.
(b) Write an assembly language program to arrange an array of numbers in ascending order.

8. (a) Draw the block diagram of the internal architecture of 8086 and explain the function of each block.

(b) Write an assembly language program to transfer a block of data to a new location.

9. Write notes on any TWO of the following :

(a) Wien bridge oscillator

(b) Magnetron

(c) J-K flip flops

(d) Memory management of 8085.
